

Name: \_\_\_\_\_  
SID: \_\_\_\_\_  
Section: \_\_\_\_\_

**Final Exam -Math 032-F '07**

The exam is 50 minutes long. No notes are permitted, but calculators are.  
Show your work.

Problem	Score out of 10
1	
2	
3	
4	
5	
6	
7	
8	
Total	

1. Find three numbers whose sample mean is 2 and whose sample variance is 3.

2. The median income for PhD recipients in the U.S. is approximately \$74,000. Give a short explanation in “everyday English” of what this means.

3. An exotically distributed set of quantities has mean 1.05 and standard deviation 0.02. Say as much as you can about the proportion of the quantities that exceeds 1.13.

4. A neurological disorder by the name of Nastiosis turns its victims into dangerous psychopaths. It affects 1 out of every 10,000 individuals. A screening test is developed which gives a positive result for 100% of those with Nastiosis and 1% of those without it. If a random person tests positive, what is the probability that he has Nastiosis?

5. Your friend draws a card from a standard shuffled deck. Without showing you the card, he tells you (truthfully) that he is holding a queen. You then draw a card from the remainder of the deck. What is the probability that you draw the queen of hearts? Hint: Break it down into mutually exclusive cases.

6. An employer claims that the mean income of his employees is \$106,000 and that the incomes are normally distributed. You take a random sample of 9 employees, and get a sample mean  $\bar{x} = \$104,000$  and a sample standard deviation of  $s = \$6,000$ . Should you doubt the claim of the employer on probabilistic grounds?

7. If you bet a dollar on black in roulette, you have a  $18/38$  chance of winning a dollar and a  $20/38$  chance of losing a dollar. Suppose you bet a dollar on black 100 times. Approximate the probability that you come away richer than when you started.



8. A small package of alphabet soup noodles contain 3  $A$ 's, 3  $B$ 's and 3  $C$ 's. You randomly draw *without replacement* 3 noodles. Find the following probabilities.

(a) You have all three letters.

(b) You have three of the same letter.

(c) You have two of one letter and one of another.

## Tables of the Normal Distribution



### Probability Content from $-\infty$ to $Z$

Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990



### Far Right Tail Probabilities

Z	P{Z to $\infty$ }	Z	P{Z to $\infty$ }	Z	P{Z to $\infty$ }	Z	P{Z to $\infty$ }
2.0	0.02275	3.0	0.001350	4.0	0.00003167	5.0	2.867 E-7
2.1	0.01786	3.1	0.0009676	4.1	0.00002066	5.5	1.899 E-8
2.2	0.01390	3.2	0.0006871	4.2	0.00001335	6.0	9.866 E-10
2.3	0.01072	3.3	0.0004834	4.3	0.00000854	6.5	4.016 E-11
2.4	0.00820	3.4	0.0003369	4.4	0.000005413	7.0	1.280 E-12

2.5	0.00621		3.5	0.0002326		4.5	0.000003398		7.5	3.191 E-14
2.6	0.004661		3.6	0.0001591		4.6	0.000002112		8.0	6.221 E-16
2.7	0.003467		3.7	0.0001078		4.7	0.000001300		8.5	9.480 E-18
2.8	0.002555		3.8	0.00007235		4.8	7.933 E-7		9.0	1.129 E-19
2.9	0.001866		3.9	0.00004810		4.9	4.792 E-7		9.5	1.049 E-21

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TABLE A3 Values of  $t_{\alpha,n}$ 

$n$	$\alpha = .10$	$\alpha = .05$	$\alpha = .025$	$\alpha = .01$	$\alpha = .005$
1	3.078	6.314	12.706	31.821	63.657
2	1.886	2.920	4.303	6.965	9.925
3	1.638	2.353	3.182	4.541	5.841
4	1.533	2.132	2.776	3.474	4.604
5	1.476	2.015	2.571	3.365	4.032
6	1.440	1.943	2.447	3.143	3.707
7	1.415	1.895	2.365	2.998	3.499
8	1.397	1.860	2.306	2.896	3.355
9	1.383	1.833	2.262	2.821	3.250
10	1.372	1.812	2.228	2.764	3.169
11	1.363	1.796	2.201	2.718	3.106
12	1.356	1.782	2.179	2.681	3.055
13	1.350	1.771	2.160	2.650	3.012
14	1.345	1.761	2.145	2.624	2.977
15	1.341	1.753	2.131	2.602	2.947
16	1.337	1.746	2.120	2.583	2.921
17	1.333	1.740	2.110	2.567	2.898
18	1.330	1.734	2.101	2.552	2.878
19	1.328	1.729	2.093	2.539	2.861
20	1.325	1.725	2.086	2.528	2.845
21	1.323	1.721	2.080	2.518	2.831
22	1.321	1.717	2.074	2.508	2.819
23	1.319	1.714	2.069	2.500	2.807
24	1.318	1.711	2.064	2.492	2.797
25	1.316	1.708	2.060	2.485	2.787
26	1.315	1.706	2.056	2.479	2.779
27	1.314	1.703	2.052	2.473	2.771
28	1.313	1.701	2.048	2.467	2.763
29	1.311	1.699	2.045	2.462	2.756
$\infty$	1.282	1.645	1.960	2.326	2.576

*Other Probabilities:*

$P\{T_8 < 2.541\} = .9825$   $P\{T_8 < 2.7\} = .9864$   $P\{T_{11} < .7635\} = .77$   $P\{T_{11} < .934\} = .81$   $P\{T_{11} < 1.66\} = .94$   $P\{T_{12} < 2.8\} = .984$ .