

1. F T T F T

2. 6, $4^x \ln 4$, f , e^x , e^4 , π

3. $\int_0^{15} |v(t)| dt$

4. With notation as in the book,

$$\Delta x = \frac{b-a}{n} = \frac{3-0}{3} = 1, \quad R_3 = \Delta x (f(1) + f(2) + f(3)) = 1(1 + 4 + 9) = 14$$

Answer: 14

5. (a) Answer: $\ln|x| + C$

(b) With the substitution $u = x^3$, one gets $\frac{du}{dx} = 3x^2$ and

$$\int x^2 e^{x^3} dx = \frac{1}{3} \int e^u du = \frac{1}{3} e^u + C = \frac{e^{x^3}}{3} + C$$

Answer: $\frac{e^{x^3}}{3} + C$

(c) Answer: $3 \tan^{-1} x + C$

6.

$$\begin{aligned} \int_{-1}^{\frac{\pi}{2}} f(x) dx &= \int_{-1}^0 f(x) dx + \int_0^{\frac{\pi}{2}} f(x) dx = \\ \int_{-1}^0 x^2 + 1 dx + \int_0^{\frac{\pi}{2}} \cos x dx &= \left(\frac{x^3}{3} + x \right) \Big|_{-1}^0 + \sin x \Big|_0^{\frac{\pi}{2}} = \frac{4}{3} + 1 = \frac{7}{3} \end{aligned}$$

Answer: $\frac{7}{3}$