

Midterm 2, Phys 30, March 21, 2008**Free Response****Each problem is worth 10 pts****Useful identities:**

$$\sin^2(x) + \cos^2(x) = 1$$

$$\sec^2(x) = \tan^2(x) + 1$$

1. Evaluate the integral.

$$\int_0^{\pi/2} \sin^3 \theta \cos^2 \theta d\theta$$

2. Evaluate the integral.

$$\int \frac{x-1}{x^2+2x} dx$$

3. Evaluate the integral.

$$\int_0^{100} \sqrt{t} \ln t dt$$

4. Evaluate the integral using the given substitution. Answer must be in terms of x.

$$\int \frac{x^3}{\sqrt{x^2+25}} dx ; x = 5 \tan \theta$$

5. Find the length of arc of the curve $x = 0$ to $x = 8/9$

$$y = 2x^{3/2} - 1$$

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Answer Section

FREE RESPONSE

1. ANS:
 $\frac{2}{15}$

PTS: 10

2. ANS:
 $\frac{3}{2} \ln(x+2) - \frac{1}{2} \ln x + c$

PTS: 10

3. ANS:
 $\frac{4000}{3} \ln 2 + \frac{4000}{3} \ln 5 - \frac{4000}{9}$

PTS: 10

4. ANS:
 $\frac{1}{3} (x^2 - 50) \sqrt{x^2 + 25} + C$

PTS: 10

5. ANS:
 $\frac{52}{27}$

PTS: 10